# Load Sharing of Piled-Raft Foundations embedded in soft to medium Clay Subjected to Vertical Loads 

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#### Abstract

Many researches have been performed on pile raft foundation in order to investigate the combined nature of raft and piles that behave as a unit. The load sharing ratio of piled raft has been studied by many researchers and mathematical formulas are achieved to predict the load sharing ratio. In the present study, the closed form equation proposed by Kyujin Choi (2014 which based on tests applied from centrifuge tests on pile raft system) is applied on the case of friction piles embedded in soft/medium clay. The load sharing ratio was calculated in case of different studied parameters and the relationships between the piled raft settlement and load sharing ratio were achieved and plotted. The studied parameters included were cohesion, number of piles, piles length, piles spacing and piles diameter. The study results concluded that the load sharing ration for all studied cases is ranging from 0.73 to 0.96 . In addition the load sharing ratio is directly proportional to number of piles, piles length, piles spacing and piles diameter and inversely proportional to piles spacing. Also it can be concluded that the cohesion of soil surrounding the piles has a little effect on the value of load sharing ratio.


Index Terms- Piled Raft System, Numerical Studies, Number Of Piles, Pile Length, Pile Diameter, Pile Spacing, Soil Cohesion.

## 1. Introduction

In the urban areas pile raft foundation system is commonly used due to many factors such as the limit of areas which lead to using high rise building. High rise water table in case of a basement is located under a given structure and a weak shear modulus of the clay soil or loose sand and using piles as settlement reducers. Pile raft foundation is the system which consists of raft and piles, in this system raft transfer the loads from the superstructure to piles and then the piles transfer their loads to the bearing stratum or to the surrounding soil by friction. Practically many researches proofed that the transmitted load is shared between piles and surrounding soil in the piled raft system.

## Experimental studies

Experimental studies have discussed the sharing load in pile raft system and also the expected settlement.
Wiesner and Brown (1980) applied an experimental study on models of raft foundations in clay soil to investigate the validity of methods based on elastic continuum theory for predicting the behavior of piled-raft foundation subjected to vertical load. Cooke (1986) presented results of model tests on piled-raft foundations. He compared the behavior of piled-raft foundations with that of un-piled raft and freestanding piled group. Horikoshi and Randolph (1996) conducted centrifuge tests on piled-raft foundation models to observe settlement of piled-raft foundations on clay soil. Also Conte (2003) carried out an experimental study using centrifuge tests to determine the effect of the variation of the raft and pile geometry on the stiffness of piled-raft foundation. Moreover Lee and Chung (2005) conducted tests on piled-raft foundations models to investigate the
effect of pile installation and interaction between the raft and the piles on the behavior of piled-raft system.

### 1.1 Theoretical studies

Many theoretical studies were studied to discuss the sharing load in pile raft system and also the expected settlement.
Wiesner and Brown (1980), Russo (1998), Mendonca and de Paiva (2000), Poulos (2001) and Small and Zhang (2002) developed an approach for analyzing the piled raft system based on elastic continuum theory.
Zhuang and Lee (1994), Prakoso and Kulhawy (2001), ElMosallamy (2002), Mendonca and da paiva (2003), Kitiyodom and Matsumoto (2003), Reul (2004), Wong and Poulos (2005) and Comodromos (2009) introduced an analysis procedure based on two dimensional and three dimensional finite element analysis.
In the conventional design of pile raft system, piles carried all the loads transferred from the superstructures to the raft and so the pile cap or the raft bearing capacity is neglected. The aim of this study to determine the load sharing of pile raft system and the factors effecting the load sharing value.

## 2. Present Numerical study

Numerical calculations were applied in the present study to determine the load sharing ratio ( $\delta$ ) in a piled-raft system where the piles are embedded in soft/medium clay soil. This study takes into account the effect of many parameters on the sharing ratio ( $\delta$ ) throughout 1500 case study. The studied parameters included pile diameter (D), pile length $\left(\mathrm{P}_{\mathrm{L}}\right)$, pile spacing ( $\left.\mathrm{P}_{\mathrm{s}}\right)$, number of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ and soil cohesion (C). The closed formula was investigated by Junhwan Lee in 2014, which is based on tests carried out by
centrifuge tests is applied to determine the sharing ratio, which means the percentage of superstructure loads transmitted via the raft and carried by piles only.
Sharing
ratio
( $\delta$ )
1/
$\left((\beta \cdot \zeta) \cdot\left(a_{p} \cdot \lambda_{B}+b_{p} \cdot\left(S / B_{r}\right) /\left(a_{r}+b_{r} \cdot\left(S / B_{r}\right)+1\right)\right.\right.$
Where $\beta$ is the load capacity interaction factor, from centrifuge tests applied on different types of clay soil and for single pile, unpiled raft, pile group and piled raft the magnitude of is $\beta=1$.
$\zeta$ is the load capacity ratio equal to $Q_{u r, u} / Q_{p g, u} . Q_{u r, u}$ (ultimate load capacity of unpiled raft), $\mathrm{Q}_{\mathrm{pg}, \mathrm{u}}$ (ultimate load capacity of pile group).
$a_{p}, b_{p}, a_{r}$ and $b_{r}$ are model parameters. From centrifuge test applied on different types of clay soil and for single pile, unpiled raft, pile group and piled raft the magnitude of $a_{p}$, $b_{p}, a_{r}$ and $b_{r}$ are $0.02,0.80,0.01$ and 0.90 respectively.
$\lambda_{B}$ is the foundation size ratio equal to PS/D (pile spacing / pile diameter).
$S$ is the settlement of piled-raft system.
$B_{r}$ is the raft width.
This closed formula based on the normalized non-linear load settlement relationship and the normalized non-linear load settlement relationship based on the hyperbolic functions of raft and piles which are investigated from centrifuge tests.

### 2.1 Parametric study

The following table presents the different values of parameters considered in the parametric study.

| No.of <br> piles <br> $\left(\mathbf{N}_{\mathbf{p}}\right)$ | Pile <br> Diameter <br> $(\mathbf{D}) \mathbf{m}$ | Pile <br> Spacing <br> $\left(\mathbf{P}_{\mathbf{s}}\right)$ | Pile <br> Length <br> $\left(\mathbf{P}_{\mathbf{L}}\right)$ | Soil <br> Cohesion <br> $(\mathrm{C}) \mathbf{K n} / \mathbf{m}^{\mathbf{2}}$ |
| :--- | :--- | :--- | :--- | :--- |
| 9 | 0.40 | 4 D | 20 D | 60 |
| 16 | 0.50 | 5 D | 25D | 80 |
| 25 | 0.60 | 6 D | 30D | 100 |
| 36 |  | 7 D | 35D |  |
| 49 |  | 8 D | 40 D |  |

## 3. Results of numerical study

### 3.1. Introduction

The mentioned closed form equation was applied to different studied cases in order to construct the relationship between load sharing ratio ( $\delta$ ) of the piled-raft system and observe the effect of the considered parameters on the ratio $(\delta)$ at any desired settlement ratio (S/D).

### 3.2. Effect of no.of piles $\left(\mathbf{N}_{p}\right)$

To investigate the effect of number of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ which varies from 9 piles to 49 piles on the relationship between load sharing ration ( $\delta$ ) and piles raft settlement (S), The parametric study were plotted in figures (1) to (8) . Each
graph represents the mentioned relationship at different values of number of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ with constant values of the other parameters Pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ), Pile length ( $\mathrm{P}_{1}$ ), Pile diameter (D), and Soil cohesion (C). Then the same investigation was repeated throughout four series. Series no. 1 shows the effect of $\left(\mathrm{N}_{\mathrm{p}}\right)$ for different studied values of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) which varies from 4 D to 8 D with the constant values of the other parameters (pile diameter, pile spacing, pile length and soil cohesion), By the same way, series no. 2 shows the effect of $\left(\mathrm{N}_{\mathrm{p}}\right)$ at different studied values of pile length ( $\mathrm{P}_{\mathrm{l}}$ ) which varies from 20D to 40D. Whereas series no. 3 represents the effect of $N_{p}$ for different studied values of pile diameter (D) ranging from 0.40 m to 0.60 m , Last series no. 4 was performed to observe the effect of $\left(\mathrm{N}_{\mathrm{p}}\right)$ for different studied values of surrounding soil cohesion (C) ranging from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$. The resulting graphical relationships represent the values of load sharing ratio ( $\delta$ ) versus raft-pile system settlement up to a limit value of (0.1D). on the other hand each graphical relationship was re-plotted specifically up to (0.02D) which is the allowable value of pile group settlement according to Egyptian Code of Practice (E.C.P). That, in turn means that the load sharing ratio ( $\delta$ ) corresponding to the settlement of ( 0.02 D ) may be considered the working load sharing ratio.

### 3.2.1 Effect of no.of piles at different values of pile spacing

Cases studied of series no. 1 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of number of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ at different values of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) varying from 4D to 8D center-line to center-line. Figures (1.a) and (1.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.1, the ( $\delta$ ) versus (S) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to S/D = 0.02 ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) increases as the number of piles beneath raft increases. In addition, it is obvious from figure (2) that the load sharing ratio ( $\delta$ ) is inversely proportional to the pile spacing $\left(\mathrm{P}_{\mathrm{s}}\right)$ for the same number of piles. For all the studied cases through the parameter $\left(\mathrm{N}_{\mathrm{p}}\right)$, it is noticed that the load sharing ratio $(\delta)$ is ranging from 0.734 to 0.957 at a settlement ratio (S/D) of 0.02, i.e. at the working load conditions.


Fig. 1.a


Fig. 1.b
Fig.1. Relationship between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and $(\delta)$ for different values of ( $\mathrm{P}_{\mathrm{s}}$ )

|  |  | $\mathrm{P}_{\mathrm{S}}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 4 D | 5 D | 6 D | 7 D | 8 D |  |
| $之$ | 9 | 0.897 | 0.850 | 0.808 | 0.769 | 0.734 |  |
|  | 16 | 0.923 | 0.880 | 0.842 | 0.806 | 0.773 |  |
|  | 25 | 0.939 | 0.901 | 0.866 | 0.833 | 0.803 |  |
|  | 36 | 0.949 | 0.916 | 0.884 | 0.854 | 0.826 |  |
|  | 49 | 0.957 | 0.926 | 0.898 | 0.871 | 0.845 |  |

Table.1. Values of ( $\delta$ ) for the relation between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and $\left(\mathrm{P}_{\mathrm{s}}\right)$


Fig.2. values of ( $\delta$ ) for the relation between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and ( $\mathrm{P}_{\mathrm{s}}$ )

### 3.2.2 Effect of no.of piles at different values of pile length

Cases studied of series no. 2 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of number of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ at different values of pile length $\left(\mathrm{P}_{1}\right)$ varying from 20D to 40D. Figures (3.a) and (3.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.2, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement $(\mathrm{S})$, and the first portion of any relationship (up to $\mathrm{S} / \mathrm{D}=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) increases as the pile length increase. In addition, it is obvious from figure (4) that the load sharing ratio ( $\delta$ ) is direct proportional to the pile length $\left(\mathrm{P}_{1}\right)$ for the same number of piles. For all the studied cases through the parameter $\left(\mathrm{N}_{\mathrm{p}}\right)$, it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.737 to 0.921 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig.3.a.


Fig.3.b.
Fig.3. Relationship between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and $(\delta)$ for different values of ( $\mathrm{P}_{\mathrm{l}}$ )

|  |  | $\mathrm{P}_{1}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 20 D | 25 D | 30 D | 35 D | 40 D |  |
| 2 | 9 | 0.737 | 0.778 | 0.808 | 0.831 | 0.849 |  |
|  | 16 | 0.780 | 0.8168 | 0.842 | 0.861 | 0.877 |  |
|  | 25 | 0.812 | 0.8438 | 0.866 | 0.883 | 0.896 |  |
|  | 36 | 0.835 | 0.864 | 0.884 | 0.899 | 0.910 |  |
|  | 49 | 0.854 | 0.879 | 0.898 | 0.911 |  |  |

Table.2. Values of ( $\delta$ ) for the relation between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and ( $\mathrm{P}_{1}$ )


Fig.4. values of $(\delta)$ for the relation between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and $\left(\mathrm{P}_{\mathrm{l}}\right)$

### 3.2.3 Effect of no.of piles at different values of pile diameter

Cases studied of series no. 3 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of number of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ at different values of pile diameter (D) varying from 0.40 m to 0.60 m . Figures (5.a) and (5.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.3, the ( $\delta$ ) versus (S) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement ( S ), and the first portion of any relationship (up to $\mathrm{S} / \mathrm{D}=0.02$ ) is
approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) is constant as the pile diameter increase. In addition, it is obvious from figure (6) that the load sharing ratio ( $\delta$ ) is constant to the pile diameter (D) for the same number of piles. For all the studied cases through the parameter $\left(\mathrm{N}_{\mathrm{p}}\right)$, it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.808 to 0.894 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 5.a


Fig. 5.b
Fig.5. Relationship between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and ( $\delta$ ) for different values of (D)


Fig.6. values of ( $\delta$ ) for the relation between ( $\mathrm{N}_{\mathrm{p}}$ ) and (D)

|  |  | 0.40 | 0.50 | 0.60 |
| :---: | :---: | :---: | :---: | :---: |
| $Z^{2}$ | 9 | 0.808 | 0.808 | 0.808 |
|  | 16 | 0.842 | 0.842 | 0.842 |
|  | 25 | 0.866 | 0.866 | 0.866 |
|  | 36 | 0.884 | 0.884 | 0.884 |
|  | 49 | 0.898 | 0.898 | 0.898 |

Table.3. Values of $(\delta)$ for the relation between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and $(\mathrm{D})$

### 3.2.4 Effect of no.of piles at different values of soil cohesion

Cases studied of series no. 4 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of number of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ at different values of soil cohesion (C) varying from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$. Figures (7.a) and (7.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.4, the ( $\delta$ ) versus (S) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to S/D = 0.02 ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) has a small increases as the soil cohesion increase. In addition, it is obvious from figure (8) that the load sharing ratio ( $\delta$ ) has a neglect able direct proportional to the soil cohesion (C) for the same number of piles. For all the studied cases through the parameter $\left(\mathrm{N}_{\mathrm{p}}\right)$, it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.806 to 0.898 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 7.a


Fig. 7.b
Fig.7. values of ( $\delta$ ) for the relation between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and $(\mathrm{C})$


Fig.8. values of ( $\delta$ ) for the relation between $\left(\mathrm{N}_{\mathrm{p}}\right)$ and (C)

|  |  | C |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 60 | 80 | 100 |
| Z | 9 | 0.806 | 0.808 | 0.809 |
|  | 16 | 0.840 | 0.842 | 0.843 |
|  | 25 | 0.865 | 0.866 | 0.867 |
|  | 36 | 0.883 | 0.883 | 0.885 |
|  | 49 | 0.896 | 0.898 | 0.898 |

Table.4. Values of ( $\delta$ ) for the relation between ( $\mathrm{N}_{\mathrm{p}}$ ) and (C)

### 3.3. Effect of pile length ( $\mathbf{P}_{\mathbf{1}}$ )

To investigate the effect of pile length ( $\mathrm{P}_{1}$ ) which varies from 20D to 40D on the relationship between load sharing ration $(\delta)$ and piles raft settlement (S), The parametric study were plotted in figures (9) to (16) . Each graph represents the mentioned relationship at different values of pile length $\left(\mathrm{P}_{1}\right)$ with constant values of the other parameters Pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ), No.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$, Pile diameter (D), and Soil cohesion (C). Then the same investigation was repeated throughout four series. Series no. 5 shows the effect of $\left(\mathrm{P}_{1}\right)$ for different studied values of pile spacing $\left(\mathrm{P}_{\mathrm{s}}\right)$ which varies from 4D to 8D with the constant values of the other parameters (pile diameter, pile spacing, no.of piles and soil cohesion), By the same way, series no. 6 shows the effect of
$\left(\mathrm{P}_{1}\right)$ at different studied values of no.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ which varies from 9 piles to 49 piles. Whereas series no. 7 represents the effect of $\mathrm{P}_{1}$ for different studied values of pile diameter (D) ranging from 0.40 m to 0.60 m , Last series no. 8 was performed to observe the effect of $\left(\mathrm{P}_{1}\right)$ for different studied values of surrounding soil cohesion (C) ranging from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$. The resulting graphical relationships represent the values of load sharing ratio ( $\delta$ ) versus raft-pile system settlement up to a limit value of ( 0.1 D ). on the other hand each graphical relationship was re-plotted specifically up to (0.02D) which is the allowable value of pile group settlement according to Egyptian Code of Practice (E.C.P). That, in turn means that the load sharing ratio $(\delta)$ corresponding to the settlement of $(0.02 \mathrm{D})$ may be considered the working load sharing ratio.

### 3.3.1 Effect of pile length at different values of pile spacing

Cases studied of series no. 5 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile length ( $\mathrm{P}_{\mathrm{l}}$ ) at different values of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) varying from 4 D to 8 D centerline to center-line. Figures (9.a) and (9.b) illustrate an example of the resulting relationships between load sharing ratios $(\delta)$ and pile raft settlement (S). for all studied cases in case series no.5, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $S / D=$ 0.02 ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) increases as the pile length beneath raft increases. In addition, it is obvious from figure (10) that the load sharing ratio ( $\delta$ ) is inversely proportional to the pile spacing $\left(\mathrm{P}_{\mathrm{s}}\right)$ for the same pile length. For all the studied cases through the parameter $\left(\mathrm{P}_{\mathrm{l}}\right)$, it is noticed that the load sharing ratio $(\delta)$ is ranging from 0.731 to 0.954 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 9.a


Fig. 9.b
Fig.9. Relationship between ( $\mathrm{P}_{1}$ ) and $(\delta)$ for different values of $\left(\mathrm{P}_{\mathrm{s}}\right)$

|  |  | $\mathrm{P}_{\mathrm{s}}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 4 D | 5 D | 6 D | 7 D | 8 D |  |
| $\approx$ | 20 D | 0.911 | 0.859 | 0.812 | 0.769 | 0.731 |  |
|  | 25 D | 0.928 | 0.884 | 0.843 | 0.807 | 0.773 |  |
|  | 30 D | 0.939 | 0.901 | 0.8665 | 0.833 | 0.803 |  |
|  | 35 D | 0.947 | 0.914 | 0.883 | 0.854 | 0.826 |  |
|  | 40 D | 0.954 | 0.924 | 0.896 | 0.869 | 0.845 |  |

Table.5. Values of ( $\delta$ ) for the relation between ( $\mathrm{P}_{1}$ ) and ( $\mathrm{P}_{\mathrm{s}}$ )


Fig.10. values of $(\delta)$ for the relation between $\left(\mathrm{P}_{1}\right)$ and $\left(\mathrm{P}_{\mathrm{s}}\right)$

### 3.3.2 Effect of pile length at different values of no.of piles

Cases studied of series no. 6 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile length ( $\mathrm{P}_{\mathrm{l}}$ ) at different values of no.of piles $\left(N_{p}\right)$ varying from 9 piles to 49 piles. Figures (11.a) and (11.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.6, the ( $\delta$ ) versus ( S ) relationships are similar in shape
and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $S / D=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) increases as the pile length increase. In addition, it is obvious from figure (12) that the load sharing ratio $(\delta)$ is direct proportional to the no.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ for the same pile length. For all the studied cases through the parameter $\left(\mathrm{P}_{1}\right)$, it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.737 to 0.921 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig.11.a


Fig.11.b
Fig.11. Relationship between $\left(\mathrm{P}_{1}\right)$ and ( $\delta$ ) for different values of $\left(\mathrm{N}_{\mathrm{p}}\right)$

|  |  | $\mathrm{N}_{\mathrm{p}}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 9 | 16 | 25 | 36 | 49 |  |
| $\approx$ | 20D | 0.737 | 0.780 | 0.812 | 0.835 | 0.854 |  |
|  | 25D | 0.778 | 0.816 | 0.843 | 0.864 | 0.879 |  |
|  | 30D | 0.808 | 0.842 | 0.866 | 0.884 | 0.898 |  |
|  | 35D | 0.831 | 0.861 | 0.883 | 0.899 | 0.911 |  |
|  | 40 D | 0.849 | 0.877 | 0.896 | 0.910 | 0.921 |  |

Table.6. Values of $(\delta)$ for the relation between $\left(\mathrm{P}_{1}\right)$ and $\left(\mathrm{N}_{\mathrm{p}}\right)$


Fig.12. values of $(\delta)$ for the relation between $\left(\mathrm{P}_{1}\right)$ and $\left(\mathrm{N}_{\mathrm{p}}\right)$

### 3.3.3 Effect of pile length at different values of pile diameter

Cases studied of series no. 6 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile length $\left(\mathrm{P}_{1}\right)$ at different values of pile diameter (D) varying from 0.40 m to 0.60 m . Figures (13.a) and (13.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.7, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $S / D=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) is constant as the pile diameter increase. In addition, it is obvious from figure (14) that the load sharing ratio $(\delta)$ is constant to the pile diameter (D) for the same pile length. For all the studied cases through the parameter $\left(\mathrm{P}_{1}\right)$, it is noticed that the load sharing ratio $(\delta)$ is ranging from 0.812 to 0.896 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 13.a


Fig. 13.b
Fig.13. Relationship between $\left(\mathrm{P}_{\mathrm{l}}\right)$ and $(\delta)$ for different values of (D)


Fig.14. values of ( $\delta$ ) for the relation between ( $\mathrm{P}_{1}$ ) and ( D )

| $\approx$ | 20D | 0.812 | 0.812 | 0.812 |
| :---: | :---: | :---: | :---: | :---: |
|  | 25 D | 0.843 | 0.843 | 0.843 |
|  | 30D | 0.866 | 0.866 | 0.866 |
|  | 35D | 0.883 | 0.883 | 0.883 |
|  | 40 D | 0.896 | 0.896 | 0.896 |

Table.7. Values of ( $\delta$ ) sharing for the relation between ( $\mathrm{P}_{1}$ ) and (D)

### 3.3.4 Effect of pile length at different values of soil cohesion

Cases studied of series no. 8 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile length ( $\mathrm{P}_{1}$ ) at different values of soil cohesion (C) varying from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$. Figures (15.a) and (15.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.8, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to S/D = 0.02 ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) has a small increases as the soil cohesion increase. In addition, it is obvious from figure (16) that the load sharing ratio ( $\delta$ ) has a neglect able direct proportional to the soil cohesion (C) for the same pile length. For all the studied cases through the parameter $\left(\mathrm{P}_{1}\right)$, it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.809 to 0.896 at a settlement ratio (S/D) of 0.02, i.e. at the working load conditions.


Fig. 15.a

| D |  |  |
| :---: | :---: | :---: |
| 0.40 | 0.50 | 0.60 |



Fig. 15.b
Fig.15. values of ( $\delta$ ) for the relation between $\left(\mathrm{P}_{1}\right)$ and $(\mathrm{C})$


Fig.16. values of ( $\delta$ ) for the relation between $\left(\mathrm{P}_{1}\right)$ and (C)

|  |  | C |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 60 | 80 | 100 |
| $\approx$ | 20D | 0.806 | 0.808 | 0.809 |
|  | 25D | 0.840 | 0.842 | 0.843 |
|  | 30D | 0.865 | 0.866 | 0.867 |
|  | 35D | 0.883 | 0.883 | 0.885 |
|  | 40 D | 0.896 | 0.898 | 0.898 |

Table.8. Values of $(\delta)$ sharing for the relation between $\left(\mathrm{P}_{1}\right)$ and (C)

Pile length $\left(\mathrm{P}_{1}\right)$, No.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$, Pile diameter (D), and Soil cohesion (C). Then the same investigation was repeated throughout four series. Series no. 9 shows the effect of $\left(\mathrm{P}_{\mathrm{s}}\right)$ for different studied values of pile length ( $\mathrm{P}_{1}$ ) which varies from 20D to 40D with the constant values of the other parameters (pile diameter, pile length, no.of piles and soil cohesion), By the same way, series no. 10 shows the effect of $\left(\mathrm{P}_{\mathrm{s}}\right)$ at different studied values of no.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ which varies from 9 piles to 49 piles. Whereas series no. 11 represents the effect of $P_{s}$ for different studied values of pile diameter (D) ranging from 4D to 8D, Last series no. 12 was performed to observe the effect of $\left(\mathrm{P}_{\mathrm{s}}\right)$ for different studied values of surrounding soil cohesion (C) ranging from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$. The resulting graphical relationships represent the values of load sharing ratio ( $\delta$ ) versus raft-pile system settlement up to a limit value of (0.1D). on the other hand each graphical relationship was re-plotted specifically up to (0.02D) which is the allowable value of pile group settlement according to Egyptian Code of Practice (E.C.P). That, in turn means that the load sharing ratio $(\delta)$ corresponding to the settlement of ( 0.02 D ) may be considered the working load sharing ratio.

### 3.4.1 Effect of pile spacing at different values of pile length

Cases studied of series no. 9 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) at different values of pile length $\left(\mathrm{P}_{\mathrm{l}}\right)$ varying from 20D to 40D. Figures (17.a) and (17.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.9, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $S / D=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) increases as the pile length beneath raft increases. In addition, it is obvious from figure (18) that the load sharing ratio ( $\delta$ ) is inversely proportional to the pile spacing $\left(\mathrm{P}_{\mathrm{s}}\right)$ for the same pile spacing. For all the studied cases through the parameter $\left(\mathrm{P}_{\mathrm{s}}\right)$, it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.731 to 0.954 at a settlement ratio (S/D) of 0.02, i.e. at the working load conditions.

### 3.4. Effect of pile spacing $\left(\mathbf{P}_{\mathrm{s}}\right)$

To investigate the effect of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) which varies from 4 D to 8 D on the relationship between load sharing ration $(\delta)$ and piles raft settlement (S), The parametric study were plotted in figures (17) to (24). Each graph represents the mentioned relationship at different values of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) with constant values of the other parameters


Fig. 17.a


Fig. 17.b
Fig.17. Relationship between ( $\mathrm{P}_{\mathrm{s}}$ ) and ( $\delta$ ) for different values of ( $\mathrm{P}_{1}$ )

|  |  | $\mathrm{P}_{1}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 20 D | 25 D | 30 D | 35 D | 40 D |  |
| $\approx$ | 4 D | 0.911 | 0.928 | 0.939 | 0.947 | 0.954 |  |
|  | 5D | 0.859 | 0.884 | 0.9012 | 0.914 | 0.924 |  |
|  | 6D | 0.812 | 0.843 | 0.866 | 0.883 | 0.896 |  |
|  | 7D | 0.769 | 0.807 | 0.833 | 0.854 | 0.869 |  |
|  | 8D | 0.731 | 0.773 | 0.803 | 0.826 | 0.845 |  |

Table.9. Values of ( $\delta$ ) for the relation between $\left(\mathrm{P}_{\mathrm{s}}\right)$ and $\left(\mathrm{P}_{\mathrm{l}}\right)$


Fig.18. values of $(\delta)$ for the relation between ( $\mathrm{P}_{\mathrm{s}}$ ) and ( $\mathrm{P}_{\mathrm{l}}$ )

### 3.4.2 Effect of pile spacing at different values of no.of piles

Cases studied of series no. 10 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) at different values of no.of piles ( $\mathrm{N}_{\mathrm{p}}$ ) varying from 9 piles to 49 piles. Figures (19.a) and (19.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.10, the ( $\delta$ ) versus (S) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement ( S ), and the first portion of any relationship (up to $\mathrm{S} / \mathrm{D}=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) decreases as the pile spacing increase. In addition, it is obvious from figure (20) that the load sharing ratio ( $\delta$ ) is inverse proportional to the no. of piles $\left(N_{p}\right)$ for the same pile spacing. For all the studied cases through the parameter ( $\mathrm{P}_{\mathrm{s}}$ ), it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.734 to 0.957 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig.19.a


Fig.19.b
Fig.19. Relationship between ( $\mathrm{P}_{\mathrm{s}}$ ) and ( $\delta$ ) for different values of $\left(\mathrm{N}_{\mathrm{p}}\right)$

|  |  | $\mathrm{N}_{\mathrm{p}}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 9 | 16 | 25 | 36 | 49 |
| $\sim$ | 4 D | 0.897 | 0.923 | 0.939 | 0.949 | 0.957 |
|  | 5D | 0.850 | 0.881 | 0.901 | 0.916 | 0.926 |
|  | 6D | 0.80 | 0.842 | 0.866 | 0.884 | 0.898 |
|  | 7D | 0.769 | 0.806 | 0.833 | 0.854 | 0.871 |
|  | 8D | 0.734 | 0.773 | 0.803 | 0.826 | 0.845 |

Table.10. Values of $(\delta)$ for the relation between $\left(\mathrm{P}_{\mathrm{s}}\right)$ and $\left(\mathrm{N}_{\mathrm{p}}\right)$


Fig.20. values of ( $\delta$ ) for the relation between ( $\mathrm{P}_{\mathrm{s}}$ ) and ( $\mathrm{N}_{\mathrm{p}}$ )

### 3.4.3 Effect of pile spacing at different values of pile diameter

Cases studied of series no. 11 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) at different values of pile diameter (D) varying from 0.40 m to 0.60 m . Figures (21.a) and (22.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.11, the ( $\delta$ ) versus (S) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $\mathrm{S} / \mathrm{D}=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) is decrease as the pile spacing increase. In addition, it is obvious from figure (22) that the load sharing ratio ( $\delta$ ) is constant to the pile diameter (D) for the same pile spacing. For all the studied cases through the parameter ( $\mathrm{P}_{\mathrm{s}}$ ), it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.803 to 0.939 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 21.a


Fig. 21.b
Fig.21. Relationship between $\left(\mathrm{P}_{\mathrm{s}}\right)$ and ( $\delta$ ) for different values of (D)

|  |  | D |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 0.40 | 0.50 | 0.60 |
| $厶^{\circ}$ | 4 D | 0.939 | 0.939 | 0.939 |
|  | 5 D | 0.901 | 0.901 | 0.90 |
|  | 6D | 0.866 | 0.866 | 0.866 |
|  | 7D | 0.833 | 0.833 | 0.833 |
|  | 8D | 0.803 | 0.803 | 0.803 |

Table.11. Values of ( $\delta$ ) for the relation between ( $\mathrm{P}_{\mathrm{s}}$ ) and (D)


Fig.22. values of ( $\delta$ ) for the relation between ( $\mathrm{P}_{\mathrm{s}}$ ) and (D)

### 3.4.4 Effect of pile spacing at different values of soil cohesion

Cases studied of series no. 12 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) at different values of soil cohesion (C) varying from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$. Figures (23.a) and (23.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.12, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion
between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to S/D = 0.02 ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) has a small increases as the soil cohesion increase. In addition, it is obvious from figure (24) that the load sharing ratio ( $\delta$ ) has a neglect able direct proportional to the soil cohesion (C) for the same pile length. For all the studied cases through the parameter $\left(\mathrm{P}_{1}\right)$, it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.809 to 0.896 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 23.a


Fig. 23.b
Fig.23. Relationship between ( $\mathrm{P}_{\mathrm{s}}$ ) and ( $\delta$ ) for different values of (C)

|  |  | C |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 60 | 80 | 100 |
| $\bumpeq$ | 4 D | 0.938 | 0.939 | 0.939 |
|  | 5D | 0.900 | 0.902 | 0.902 |
|  | 6D | 0.865 | 0.866 | 0.867 |
|  | 7D | 0.832 | 0.833 | 0.834 |
|  | 8D | 0.801 | 0.803 | 0.804 |

Table.12. Values of ( $\delta$ ) for the relation between ( $\mathrm{P}_{\mathrm{s}}$ ) and (C)


Fig.24. values of $(\delta)$ for the relation between $\left(\mathrm{P}_{\mathrm{s}}\right)$ and (C)

### 3.5. Effect of soil cohesion (C)

To investigate the effect of soil cohesion (C) which varies from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$ on the relationship between load sharing ration ( $\delta$ ) and piles raft settlement (S), The parametric study were plotted in figures (25) to (32) . Each graph represents the mentioned relationship at different values of soil cohesion (C) with constant values of the other parameters Pile length $\left(\mathrm{P}_{1}\right)$, No.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$, Pile diameter (D), and pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ). Then the same investigation was repeated throughout four series. Series no. 13 shows the effect of $(\mathrm{C})$ for different studied values of pile length $\left(\mathrm{P}_{\mathrm{l}}\right)$ which varies from 20D to 40D with the constant values of the other parameters (pile diameter, pile spacing, no.of piles and soil cohesion), By the same way, series no. 14 shows the effect of (C) at different studied values of no.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ which varies from 9 piles to 49 piles. Whereas series no. 15 represents the effect of $C$ for different studied values of pile diameter (D) ranging from 0.40 m to 0.60 m , Last series no. 16 was performed to observe the effect of (C) for different studied values of pile spacing $\left(\mathrm{P}_{\mathrm{s}}\right)$ ranging from 4 D to 8 D . The resulting graphical relationships represent the values of load sharing ratio ( $\delta$ ) versus raft-pile system settlement up to a limit value of (0.1D). on the other hand each graphical relationship was re-plotted specifically up to (0.02D) which is the allowable value of pile group settlement according to Egyptian Code of Practice (E.C.P). That, in turn means that the load sharing ratio $(\delta)$ corresponding to the settlement of (0.02D) may be considered the working load sharing ratio.

### 3.5.1 Effect of soil cohesion (C) at different values of pile length

Cases studied of series no. 13 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of soil cohesion (C) at different values of pile length $\left(\mathrm{P}_{\mathrm{l}}\right)$ varying from 20D to 40D. Figures (25.a) and (25.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.13, the
behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $S / D=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) increases as the soil cohesion increases with small values. In addition, it is obvious from figure (26) that the load sharing ratio ( $\delta$ ) is directly proportional to the soil cohesion (C) for the same pile length. For all the studied cases through the parameter (C), it is noticed that the load sharing ratio $(\delta)$ is ranging from 0.801 to 0.939 at a settlement ratio (S/D) of 0.02, i.e. at the working load conditions.


Fig. 25.a


Fig. 25.b
Fig.25. Relationship between (C) and ( $\delta$ ) for different values of ( $\mathrm{P}_{\mathrm{l}}$ )

|  |  | $\mathrm{P}_{1}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 20 D | 25 D | 30 D | 35 D | 40 D |
| $\cup$ | 60 | 0.938 | 0.900 | 0.865 | 0.832 | 0.801 |
|  | 80 | 0.939 | 0.901 | 0.866 | 0.833 | 0.803 |


|  | 100 | 0.939 | 0.902 | 0.867 | 0.8345 | 0.804 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Table.13. Values of ( $\delta$ ) for the relation between (C) and ( $\mathrm{P}_{\mathrm{l}}$ )


Fig.26. values of $(\delta)$ for the relation between ( C ) and ( $\mathrm{P}_{1}$ )

### 3.5.2 Effect of soil cohesion at different values of no.of piles

Cases studied of series no. 14 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of soil cohesion (C) at different values of no.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ varying from 9 piles to 49 piles. Figures (27.a) and (27.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.14, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $\mathrm{S} / \mathrm{D}=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) increases as the soil cohesion increase with small values. In addition, it is obvious from figure (28) that the load sharing ratio ( $\delta$ ) is directly proportional to the no. of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ for the same soil cohesion. For all the studied cases through the parameter $(\mathrm{C})$, it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.734 to 0.957 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig.27.a


Fig.27.b
Fig.27. Relationship between (C) and ( $\delta$ ) for different values of $\left(\mathrm{N}_{\mathrm{p}}\right)$

|  |  | $\mathrm{N}_{\mathrm{p}}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 9 | 16 | 25 | 36 | 49 |  |
| $\cup$ | 60 | 0.806 | 0.840 | 0.865 | 0.883 | 0.896 |  |
|  | 80 | 0.808 | 0.842 | 0.866 | 0.884 | 0.898 |  |
|  | 100 | 0.809 | 0.843 | 0.867 | 0.885 | 0.898 |  |

Table.14. Values of ( $\delta$ )for the relation between (C) and ( $\mathrm{N}_{\mathrm{p}}$ )


Fig.28. values of $(\delta)$ for the relation between $(\mathrm{C})$ and $\left(\mathrm{N}_{\mathrm{p}}\right)$

### 3.5.3 Effect of soil cohesion at different values of pile diameter

Cases studied of series no. 15 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of soil cohesion (C) at different values of pile diameter (D) varying from 0.40 m to 0.60 m . Figures (29.a) and (29.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.15, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportional between the load sharing ratio ( $\delta$ ) and piled-raft settlement $(\mathrm{S})$, and the first portion of any relationship (up to $\mathrm{S} / \mathrm{D}=$ 0.02 ) is approximately linear. At the same settlement ratio $(\mathrm{S} / \mathrm{D})$, the load sharing ratio ( $\delta$ ) is constant as the pile diameter increase. In addition, it is obvious from figure (30) that the load sharing ratio ( $\delta$ ) is constant to the pile diameter (D) for the same soil cohesion. For all the studied cases through the parameter (C), it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.865 to 0.867 at a settlement ratio (S/D) of 0.02, i.e. at the working load conditions.


Fig. 29.a


Fig. 29.b
Fig.29. Relationship between ( $\mathrm{P}_{\mathrm{s}}$ ) and ( $\delta$ ) for different values of (D)

|  |  | D |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 0.40 | 0.50 | 0.60 |
| $\cup$ | 60 | 0.865 | 0.865 | 0.865 |
|  | 80 | 0.866 | 0.866 | 0.866 |
|  | 100 | 0.867 | 0.867 | 0.867 |

Table.15. Values of ( $\delta$ ) for the relation between (C) and (D)


Fig.30. values of ( $\delta$ ) for the relation between (C) and (D)

### 3.5.4 Effect of soil cohesion at different values of pile spacing

Cases studied of series no. 16 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of soil cohesion (C) at different values of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) varying from 4 D to 8 D center to center. Figures (31.a) and (31.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.16, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $S / D=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ )increases as the soil cohesion increase with small value. In addition, it is obvious from figure (32) that the load sharing ratio ( $\delta$ ) has an inverse proportional to the soil cohesion (C) for the same pile spacing. For all the studied cases through the parameter (C), it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.809 to 0.896 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 31.a


Fig. 31.b
Fig.31. Relationship between (C) and ( $\delta$ ) for different values of ( $\mathrm{P}_{\mathrm{s}}$ )

|  |  | $\mathrm{P}_{\mathrm{s}}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 4 D | 5 D | 6 D | 7 D | 8 D |
| $\cup$ | 60 | 0.93 | 0.900 | 0.865 | 0.832 | 0.801 |
|  | 80 | 0.939 | 0.901 | 0.866 | 0.833 | 0.803 |
|  | 100 | 0.939 | 0.902 | 0.867 | 0.834 | 0.804 |

Table.16. Values of ( $\delta$ ) for the relation between ( C ) and ( $\mathrm{P}_{\mathrm{s}}$ )


Fig.32. values of $(\delta)$ for the relation between $(\mathrm{C})$ and $\left(\mathrm{P}_{\mathrm{s}}\right)$

To investigate the effect of pile diameter (D) which varies from 0.40 m to 0.60 m on the relationship between load sharing ration ( $\delta$ ) and piles raft settlement (S), the parametric study were plotted in figures (33) to (40). Each graph represents the mentioned relationship at different values of pile diameter ( D ) with constant values of the other parameters Pile length $\left(\mathrm{P}_{1}\right)$, No.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$, Soil cohesion $(\mathrm{C})$, and pile spacing $\left(\mathrm{P}_{\mathrm{s}}\right)$. Then the same investigation was repeated throughout four series. Series no. 17 shows the effect of (D) for different studied values of pile length ( $\mathrm{P}_{1}$ ) which varies from 20D to 40D with the constant values of the other parameters (pile spacing, no.of piles and soil cohesion), By the same way, series no. 18 shows the effect of (D) at different studied values of no.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ which varies from 9 piles to 49 piles. Whereas series no. 19 represents the effect of D for different studied values of soil cohesion (C) ranging from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$, Last series no. 20 was performed to observe the effect of (D) for different studied values of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) ranging from 4 D to 8 D . The resulting graphical relationships represent the values of load sharing ratio ( $\delta$ ) versus raft-pile system settlement up to a limit value of (0.1D). on the other hand each graphical relationship was re-plotted specifically up to (0.02D) which is the allowable value of pile group settlement according to Egyptian Code of Practice (E.C.P). That, in turn means that the load sharing ratio ( $\delta$ ) corresponding to the settlement of (0.02D) may be considered the working load sharing ratio.

### 3.6.1 Effect of pile diameter (D) at different values of pile length

Cases studied of series no. 17 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile diameter (D) at different values of pile length $\left(\mathrm{P}_{1}\right)$ varying from 20D to 40D. Figures (33.a) and (33.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.17, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement ( S ), and the first portion of any relationship (up to $\mathrm{S} / \mathrm{D}=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio $(\delta)$ is constant with the increase of pile diameter. In addition, it is obvious from figure (34) that the load sharing ratio $(\delta)$ is directly proportional to the pile diameter (D) for the same pile length. For all the studied cases through the parameter (D), it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.812 to 0.896 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 33.a


Fig. 33.b
Fig.33. Relationship between (D) and ( $\delta$ ) for different values of ( $\mathrm{P}_{1}$ )

|  |  | $\mathrm{P}_{1}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 20 D | 25 D | 30 D | 35 D | 40 D |  |
| $\sim$ | 0.40 | 0.812 | 0.843 | 0.866 | 0.883 | 0.896 |  |
|  | 0.50 | 0.812 | 0.843 | 0.866 | 0.883 | 0.896 |  |
|  | 0.60 | 0.812 | 0.843 | 0.866 | 0.883 | 0.896 |  |

Table.17. Values of ( $\delta$ ) for the relation between ( D ) and ( $\mathrm{P}_{\mathrm{l}}$ )


Fig.34. Relationship between (D) and ( $\delta$ ) for different values of ( $\mathrm{P}_{1}$ )

### 3.6.2 Effect of pile diameter at different values of no.of piles

Cases studied of series no. 18 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile diameter (D) at different values of no.of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ varying from 9 piles to 49 piles. Figures (35.a) and (35.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.18, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $S / D=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) is constant with the increase of pile diameter. In addition, it is obvious from figure (36) that the load sharing ratio $(\delta)$ is directly proportional to the no. of piles $\left(\mathrm{N}_{\mathrm{p}}\right)$ for the same pile diameter. For all the studied cases through the parameter (D), it is noticed that the load sharing ratio ( $\square$ is ranging from 0.734 to 0.957 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig.35.a


Fig.35.b
Fig.35. Relationship between (D) and ( $\delta$ ) for different values of ( $\mathrm{N}_{\mathrm{p}}$ )

|  |  | $\mathrm{N}_{\mathrm{p}}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 9 | 16 | 25 | 36 | 49 |
| $\triangleright$ | 0.40 | 0.808 | 0.842 | 0.866 | 0.884 | 0.898 |
|  | 0.50 | 0.808 | 0.842 | 0.866 | 0.884 | 0.898 |
|  | 0.60 .884 | 0.808 | 0.842 | 0.866 |  |  |

Table.18. Values of ( $\delta$ ) for the relation between (D) and ( $\mathrm{N}_{\mathrm{p}}$ )


Fig.36. values of $(\delta)$ for the relation between (D) and $\left(N_{p}\right)$

### 3.6.3 Effect of pile diameter at different values of soil cohesion

Cases studied of series no. 19 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile diameter (D) at different values of soil cohesion (C) varying from $60 \mathrm{KN} / \mathrm{m}^{2}$ to $100 \mathrm{KN} / \mathrm{m}^{2}$. Figures (37.a) and (37.b) illustrate an example of the resulting relationships between load sharing ratios $(\delta)$ and pile raft settlement (S). for all studied cases in case series no.19, the ( $\delta$ ) versus ( S ) relationships are similar in shape and behavior. Many observations can be observed
from these relationships. There is an inverse proportional between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to S/D = 0.02 ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) is constant as the pile diameter increase. In addition, it is obvious from figure (38) that the load sharing ratio ( $\delta$ ) is increase with the increase of soil cohesion. For all the studied cases through the parameter (D), it is noticed that the load sharing ratio ( $\delta$ ) is ranging from 0.865 to 0.867 at a settlement ratio (S/D) of 0.02 , i.e. at the working load conditions.


Fig. 37.a


Fig. 37.b
Fig.37. Relationship between (D) and ( $\delta$ ) for different values of (C)

| C |  |  |
| :--- | :--- | :--- |
| 60 | 80 | 100 |


| $\sim$ | 0.40 | 0.865 | 0.866 | 0.867 |
| :--- | :--- | :--- | :--- | :--- |
|  | 0.50 | 0.865 | 0.866 | 0.867 |
|  | 0.60 | 0.865 | 0.866 | 0.867 |

Table.19. Values of ( $\delta$ ) for the relation between (D) and (C)


Fig.38. values of ( $\delta$ ) for the relation between (D) and (C)

### 3.6.4 Effect of pile diameter at different values of pile spacing

Cases studied of series no. 20 were numerically studied by applying the closed form equation suggested by (Junhwan Lee in 2014) to calculate the load sharing ratio ( $\delta$ ) taking into account the variation of pile diameter (D) at different values of pile spacing ( $\mathrm{P}_{\mathrm{s}}$ ) varying from 4D to 8D. Figures (39.a) and (39.b) illustrate an example of the resulting relationships between load sharing ratios ( $\delta$ ) and pile raft settlement (S). for all studied cases in case series no.20, the ( $\delta$ ) versus (S) relationships are similar in shape and behavior. Many observations can be observed from these relationships. There is an inverse proportion between the load sharing ratio ( $\delta$ ) and piled-raft settlement (S), and the first portion of any relationship (up to $S / D=0.02$ ) is approximately linear. At the same settlement ratio (S/D), the load sharing ratio ( $\delta$ ) is constant with the increase of pile diameter. In addition, it is obvious from figure (40) that the load sharing ratio ( $\delta$ ) has a direct proportional to the pile diameter (C) for the same pile spacing. For all the studied cases through the parameter (D), it is noticed that the load sharing ratio $(\delta)$ is ranging from 0.803 to 0.939 at a settlement ratio (S/D) of 0.02, i.e. at the working load conditions.


Fig. 39.a


Fig. 39.b
Fig.39. Relationship between (D) and ( $\delta$ ) for different values of ( $\mathrm{P}_{\mathrm{s}}$ )

|  |  | $\mathrm{P}_{\mathrm{s}}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 4 D | 5 D | 6 D | 7 D |  |
| $\sim$ | 0.40 | 0.939 | 0.901 | 0.866 | 0.833 |  |
|  |  |  |  |  |  |  |
|  | 0.50 | 0.939 | 0.901 | 0.866 | 0.833 |  |
|  | 0.60 | 0.939 | 0.901 | 0.866 | 0.833 |  |

Table.20. Values of ( $\delta$ ) for the relation between (D) and ( $\mathrm{P}_{\mathrm{s}}$ )

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Fig.40. values of $(\delta)$ for the relation between $(\mathrm{D})$ and $\left(\mathrm{P}_{\mathrm{s}}\right)$

## 4. Conclusion

- The relation between load sharing and pile diameter, pile length, number of piles, cohesion and pile spacing is non-linear, but the first portion of the graph between load sharing and piled raft system settlement is linear with maximum value of settlement equal to 0.02 D .
- Some parameters have no effect on the load sharing such as pile diameter.
- Some parameters have small effect on load sharing such as soil cohesion.
- Some parameters have significant effect on load sharing such as pile length, number of piles and pile spacing.
- The relation between load sharing and pile length, pile diameter, number of piles and cohesion is direct proportion.
- The relation between load sharing and pile spacing is inverse proportion.
- The range of load sharing values can be summarized as follows:

| parameters | Ranging <br> values | Variable parameters |
| :--- | :--- | :--- |
| $\mathrm{N}_{\mathrm{p}}$ versus $\mathrm{P}_{1}$ | 0.737 to <br> 0.921 | At $\mathrm{N}_{\mathrm{p}}=9$ piles and $\mathrm{P}_{1}=20 \mathrm{D}$ to <br> $\mathrm{N}_{\mathrm{p}}=49$ piles and $\mathrm{P}_{\mathrm{l}}=40 \mathrm{D}$ |
| $\mathrm{N}_{\mathrm{p}}$ versus $\mathrm{P}_{\mathrm{s}}$ | 0.734 to <br> 0.957 | At $\mathrm{N}_{\mathrm{p}}=9$ piles and $\mathrm{P}_{\mathrm{s}}=8 \mathrm{D}$ to <br> $\mathrm{N}_{\mathrm{p}}=49$ piles and $\mathrm{P}_{\mathrm{s}}=4 \mathrm{D}$ |
| $\mathrm{N}_{\mathrm{p}}$ versus C | 0.806 to <br> 0.898 | At $\mathrm{N}_{\mathrm{p}}=9$ piles and $\mathrm{C}=60 \mathrm{KN} /$ <br> $\mathrm{m}^{2}$ to $\mathrm{N}_{\mathrm{p}}=49$ piles and $\mathrm{C}=$ <br> $100 \mathrm{KN} / \mathrm{m}^{2}$ |
|  | 0.808 to <br> 0.898 | At $\mathrm{N}_{\mathrm{p}}=9$ piles and $\mathrm{D}=0.40 \mathrm{~m}$ to <br> $\mathrm{N}_{\mathrm{p}}=49$ piles and $\mathrm{D}=0.60 \mathrm{~m}$ |
| $\mathrm{P}_{1}$ versus $\mathrm{N}_{\mathrm{p}}$ | 0.737 to <br> 0.921 | At $\mathrm{P}_{1}=20 \mathrm{D}$ and $\mathrm{N}_{\mathrm{p}}=9$ piles to <br> $\mathrm{P}_{1}=40 \mathrm{D}$ and $\mathrm{N}_{\mathrm{p}}=49$ piles |
| $\mathrm{P}_{1}$ versus $\mathrm{P}_{\mathrm{s}}$ | 0.731 to <br> 0.953 | At $\mathrm{P}_{1}=20 \mathrm{D}$ and $\mathrm{P}_{\mathrm{s}}=8 \mathrm{D}$ to $\mathrm{P}_{1}=$ <br> 40 D and $\mathrm{P}_{\mathrm{s}}=4 \mathrm{D}$ |
| $\mathrm{P}_{1}$ versus C | 0.809 to <br> 0.896 | At $\mathrm{P}_{1}=20 \mathrm{D}$ and $\mathrm{C}=60 \mathrm{KN} / \mathrm{m}^{2}$ <br> to $P_{1}=40 \mathrm{D}$ and $\mathrm{C}=100 \mathrm{KN} / \mathrm{m}^{2}$ |
| $\mathrm{P}_{1}$ versus D | 0.812 to <br> 0.896 | At $\mathrm{P}_{1}=20 \mathrm{D}$ and $\mathrm{D}=0.40 \mathrm{~m}$ to $\mathrm{P}_{1}$ <br> $=40 \mathrm{D}$ and $\mathrm{D}=0.60 \mathrm{~m}$ |


| $\mathrm{P}_{\mathrm{s}}$ versus $\mathrm{N}_{\mathrm{p}}$ | $\begin{aligned} & \hline 0.734 \text { to } \\ & 0.957 \\ & \hline \end{aligned}$ | At $P_{s}=8 \mathrm{D}$ and $\mathrm{N}_{\mathrm{p}}=9$ piles to $\mathrm{P}_{\mathrm{s}}=4 \mathrm{D}$ and $\mathrm{N}_{\mathrm{p}}=49$ piles |
| :---: | :---: | :---: |
| $P_{s}$ versus $P_{1}$ | $\begin{aligned} & \hline 0.731 \text { to } \\ & 0.954 \end{aligned}$ | At $P_{s}=8 \mathrm{D}$ and $\mathrm{P}_{\mathrm{l}}=20 \mathrm{D}$ to $\mathrm{P}_{\mathrm{s}}=$ 4 D and $\mathrm{P}_{1}=40 \mathrm{D}$ |
| $P_{\text {s }}$ versus $C$ | $\begin{aligned} & 0.801 \text { to } \\ & 0.939 \end{aligned}$ | At $P_{s}=8 \mathrm{D}$ and $\mathrm{C}=60 \mathrm{KN} / \mathrm{m}^{2}$ to $P_{s}=4 \mathrm{D}$ and $\mathrm{C}=100 \mathrm{KN} / \mathrm{m}^{2}$ |
| $P_{\text {s }}$ versus D | $\begin{aligned} & \hline 0.803 \text { to } \\ & 0.939 \end{aligned}$ | At $P_{s}=8 \mathrm{D}$ and $\mathrm{D}=0.40 \mathrm{~m}$ to $\mathrm{P}_{\mathrm{s}}$ $=4 \mathrm{D}$ and $\mathrm{D}=0.60 \mathrm{~m}$ |
| D versus $\mathrm{N}_{\mathrm{p}}$ | $\begin{aligned} & \hline 0.808 \text { to } \\ & 0.898 \end{aligned}$ | At $\mathrm{D}=0.40 \mathrm{~m}$ and $\mathrm{N}_{\mathrm{p}}=9$ piles to $\mathrm{D}=0.60 \mathrm{~m}$ and $\mathrm{N}_{\mathrm{p}}=49$ piles |
| $D$ versus $\mathrm{P}_{\text {s }}$ | $\begin{aligned} & \hline 0.812 \text { to } \\ & 0.896 \end{aligned}$ | At $\mathrm{D}=0.40 \mathrm{~m}$ and $\mathrm{P}_{\mathrm{s}}=8 \mathrm{D}$ to D $=0.60 \mathrm{~m}$ and $\mathrm{P}_{\mathrm{s}}=4 \mathrm{D}$ |
| D versus C | $\begin{aligned} & 0.803 \text { to } \\ & 0.939 \end{aligned}$ | $\begin{aligned} & \text { At } \mathrm{D}=0.40 \mathrm{~m} \text { and } \mathrm{C}=60 \mathrm{KN} / \\ & \mathrm{m}^{2} \text { to } \mathrm{D}=0.60 \mathrm{~m} \text { and } \mathrm{C}= \\ & 100 \mathrm{KN} / \mathrm{m}^{2} \end{aligned}$ |
| D versus $\mathrm{P}_{1}$ | $\begin{aligned} & 0.865 \text { to } \\ & 0.867 \end{aligned}$ | $\begin{aligned} & \text { At } D=0.40 \mathrm{~m} \text { and } P_{l}=20 \mathrm{D} \text { to } D \\ & =0.60 \mathrm{~m} \text { and } P_{1}=40 \mathrm{D} \end{aligned}$ |
| C versus $\mathrm{N}_{\mathrm{p}}$ | $\begin{aligned} & 0.808 \text { to } \\ & 0.898 \end{aligned}$ | At $\mathrm{C}=60 \mathrm{KN} / \mathrm{m}^{2}$ and $\mathrm{N}_{\mathrm{p}}=9$ piles to $\mathrm{C}=100 \mathrm{KN} / \mathrm{m}^{2}$ and $\mathrm{N}_{\mathrm{p}}=49$ piles |
| C versus $\mathrm{P}_{\text {s }}$ | $\begin{aligned} & 0.812 \text { to } \\ & 0.896 \end{aligned}$ | At $\mathrm{C}=60 \mathrm{KN} / \mathrm{m}^{2}$ and $\mathrm{P}_{\mathrm{s}}=8 \mathrm{D}$ to $\mathrm{C}=100 \mathrm{KN} / \mathrm{m}^{2}$ and $\mathrm{P}_{\mathrm{s}}=4 \mathrm{D}$ |
| $C$ versus D | $\begin{aligned} & \hline 0.803 \text { to } \\ & 0.939 \end{aligned}$ | $\begin{aligned} & \text { At } \mathrm{C}=60 \mathrm{KN} / \mathrm{m}^{2} \text { and } \mathrm{D}=0.40 \mathrm{~m} \\ & \text { to } \mathrm{C}=100 \mathrm{KN} / \mathrm{m}^{2} \text { and } \mathrm{D}= \\ & 0.60 \mathrm{~m} \end{aligned}$ |
| $C$ versus $\mathrm{P}_{1}$ | $\begin{aligned} & \hline 0.865 \text { to } \\ & 0.867 \end{aligned}$ | At $\mathrm{C}=60 \mathrm{KN} / \mathrm{m}^{2}$ and $\mathrm{P}_{1}=20 \mathrm{D}$ to $C=100 \mathrm{KN} / \mathrm{m}^{2}$ and $\mathrm{P}_{1}=40 \mathrm{D}$ |

From 1500 case study applied on piled raft foundation the value of load sharing equal to (1E-5X + 0.7926 ).
Where $\mathrm{X}=\left(\mathrm{D} \cdot \mathrm{C} \cdot \mathrm{N}_{\mathrm{p}} \cdot \mathrm{P}_{\mathrm{l}} / \mathrm{P}_{\mathrm{s}}\right)$


Fig.41. Load sharing relationship

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